





2.

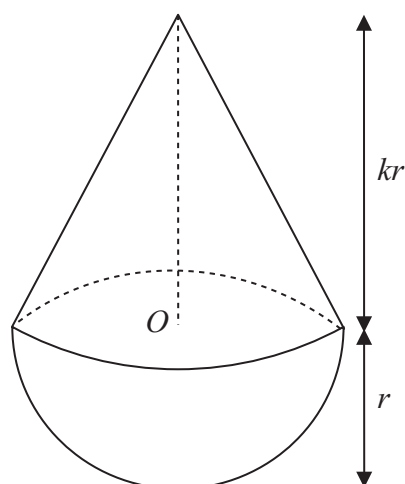


Figure 1

A uniform solid consists of a right circular cone of radius  $r$  and height  $kr$ , where  $k > \sqrt{3}$ , fixed to a hemisphere of radius  $r$ . The centre of the plane face of the hemisphere is  $O$  and this plane face coincides with the base of the cone, as shown in Figure 1.

(a) Show that the distance of the centre of mass of the solid from  $O$  is

$$\frac{(k^2 - 3)r}{4(k + 2)} \quad (5)$$

The point  $A$  lies on the circumference of the base of the cone. The solid is suspended by a string attached at  $A$  and hangs freely in equilibrium. The angle between  $AO$  and the vertical is  $\theta$ , where  $\tan \theta = \frac{11}{14}$

(b) Find the value of  $k$ .

(4)

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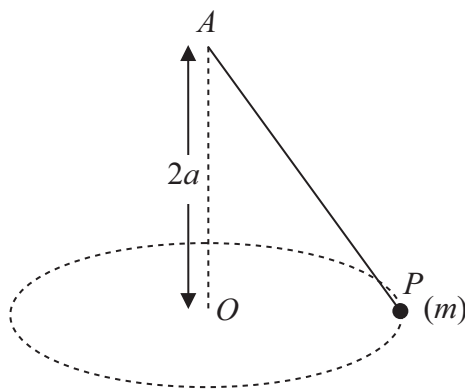


Figure 2

A particle  $P$  of mass  $m$  is attached to one end of a light elastic string, of natural length  $2a$  and modulus of elasticity  $6mg$ . The other end of the string is attached to a fixed point  $A$ . The particle moves with constant speed  $v$  in a horizontal circle with centre  $O$ , where  $O$  is vertically below  $A$  and  $OA = 2a$ , as shown in Figure 2.

(a) Show that the extension in the string is  $\frac{2}{5}a$ . (6)

(b) Find  $v^2$  in terms of  $a$  and  $g$ . (5)

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**Question 4 continued**

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6.

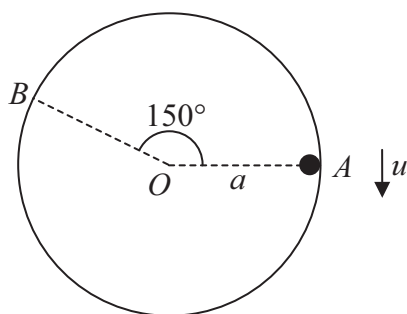


Figure 3

A smooth hollow cylinder of internal radius  $a$  is fixed with its axis horizontal. A particle  $P$  moves on the inner surface of the cylinder in a vertical circle with radius  $a$  and centre  $O$ , where  $O$  lies on the axis of the cylinder. The particle is projected vertically downwards with speed  $u$  from point  $A$  on the circle, where  $OA$  is horizontal. The particle first loses contact with the cylinder at the point  $B$ , where  $\angle AOB = 150^\circ$ , as shown in Figure 3. Given that air resistance can be ignored,

(a) show that the speed of  $P$  at  $B$  is  $\sqrt{\left(\frac{ag}{2}\right)}$ , (3)

(b) find  $u$  in terms of  $a$  and  $g$ . (4)

After losing contact with the cylinder,  $P$  crosses the diameter through  $A$  at the point  $D$ . At  $D$  the velocity of  $P$  makes an angle  $\theta^\circ$  with the horizontal.

(c) Find the value of  $\theta$ . (7)

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**Question 6 continued**

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7. A particle  $P$  of mass  $1.5$  kg is attached to the mid-point of a light elastic string of natural length  $0.30$  m and modulus of elasticity  $\lambda$  newtons. The ends of the string are attached to two fixed points  $A$  and  $B$ , where  $AB$  is horizontal and  $AB = 0.48$  m. Initially  $P$  is held at rest at the mid-point,  $M$ , of the line  $AB$  and the tension in the string is  $240$  N.

(a) Show that  $\lambda = 400$  (3)

The particle is now held at rest at the point  $C$ , where  $C$  is  $0.07$  m vertically below  $M$ . The particle is released from rest at  $C$ .

(b) Find the magnitude of the initial acceleration of  $P$ . (6)

(c) Find the speed of  $P$  as it passes through  $M$ . (6)

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